

BIG DATA

UNIT - 3

In Memory Computation

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Hadoop Challenges

- No iterative support from language
- Must do manually

SCALA

- SCALable LAnguage
- Object-oriented, compiled into Java bytecode (runs on JVM)

hello.scala compiled → scala.class

- Can reference Java libraries
- Blends OO and FP (functional programming)
- Strongly statically typed

What's wrong with Java?

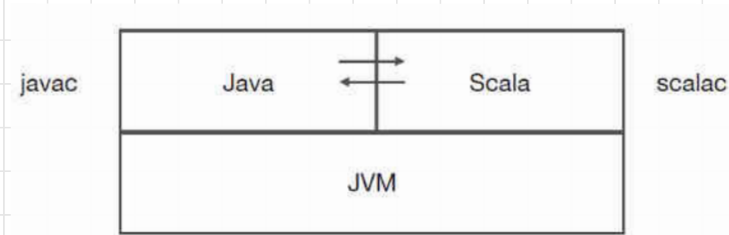
- Verbose (boilerplate)
- Not designed to be very concurrent (before Java 5+)

What's right with Java?

- Popular
- OO
- Strongly typed
- Library of classes — large
- JVM — platform independent

Java vs Scala

- Almost completely interoperable



SCALA

```
// Declaring variables
var x: Int = 7 // explicit type
var x = 7     // type inferred
val y = "hi"  // read-only (constant)

// Functions
def square(x: Int): Int = x*x

def square(x: Int): Int = {
  x*x
}

def announce(text: String) = {
  println(text)
}
```

JAVA

```
class Test {
  public static void main(String[] args) {
    int x = 7;

    final String y = "hi";
  }
}

class Example {
  int square(int x) {
    return x*x;
  }

  void announce(String text) {
    System.out.println(text);
  }
}
```

- no return keyword
- features similar to JS & python

Major Differences

1. Minimal verbosity

2. Referential Transparency

- **type inferencing** in scala
- compiler checks type of subexpressions, atomic values

3. Concurrency

- Actor model
- Akka — open-source framework for Actor-based concurrency

4. Functional Programming

- Higher order functions that can return another function
- Nested functions

1. Minimal Verbosity

- Getters & setters (note: ppt link does not work; objectmentor has been moved to <http://cleancoder.com/>)

Java

```
class Person {
    private String firstName;
    private String lastName;
    private int age;

    public Person(String firstName, String lastName, int age) {
        this.firstName = firstName;
        this.lastName = lastName;
        this.age = age;
    }

    public void setFirstName(String firstName) { this.firstName = firstName; }
    public String getFirstName() { return this.firstName; }

    public void setLastName(String lastName) { this.lastName = lastName; }
    public String getLastName() { return this.lastName; }

    public void setAge(int age) { this.age = age; }
    public int getAge() { return this.age; }
}
```

- Scala (automatic)

```
class Person(var firstName: String, var lastName: String, var age: Int)
```

2. Type Inferencing

- Java is statically typed
 - type errors caught by compiler
- Ruby & Python do not require declared types
 - harder to debug
 - not type safe
- Scala is statically typed but it uses type inferencing
 - type errors caught by compiler
 - <https://docs.scala-lang.org/tour/type-inference.html>

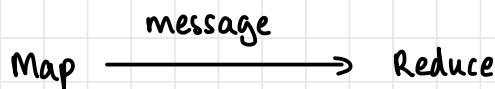
```
val collegeName = "PES University" // const reference  
def squareOf(x: Int) : x * x // def method that cannot be reassigned
```

Consistency

- Java: every value is a type, except primitive types (int, bool) for efficiency reasons
- Scala: every value is an object; compiler turns into primitives for efficiency
- Java has operators & methods with different syntaxes
- In Scala, operators are methods and either syntax can be used

3. Concurrency

- **Concurrency vs parallelism**
 - **Concurrency** creates illusion of parallelism; can execute multiple threads on the same core
 - **Concurrency** achieved through context switching
 - **Parallelism** requires multiple cores to run multiple computations simultaneously
- **Fine-grained concurrency**: frequent interactions between threads working together
 - difficult to implement right
 - requires **locks** on shared resources
- **Coarse-grained concurrency**: infrequent interactions between largely independent sequential processes
 - easier to get right
 - map-reduce
 - not at cycle level
- **Java** 5 & 6 — reasonable support for Fine-grained concurrency
- **Scala** has access to the Java API
- **Scala** also has Actors for coarse-grained parallelism
 - Sending messages using `send !` Abstraction



4. Functional Programming

- Problem with concurrency: acquire locks
- If prog language does not allow modification of variables, locks not required
- Functional programming languages use only immutable data (eg: ML, OCaml, Haskell, lisp)
- Difficult to learn
- Scala is an impure functional language — can program functionally but not forced upon you
- Features
 - (a) Immutable
 - functional operations create new structures and do not modify existing structures
 - (b) Program implicitly captures data flow
 - (c) Order of operations unimportant
 - (d) Functions
 - are objects
 - arguments
 - can be returned
 - can operate on collections

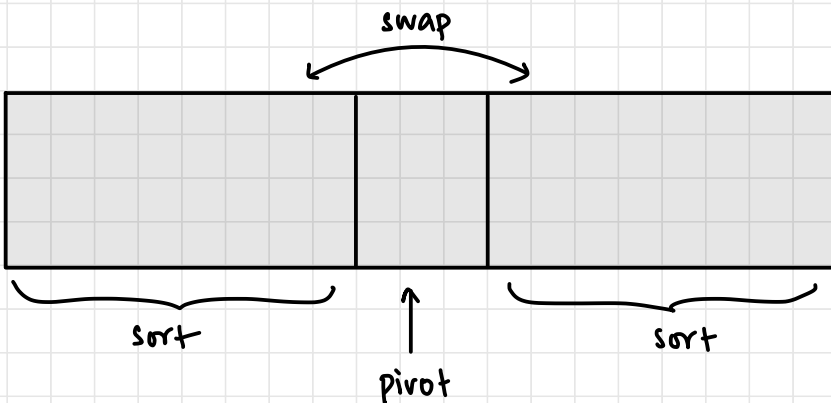
• Quicksort in Scala - Java style

```
def sort(xs: Array[Int]) {  
  def swap(i: Int, j: Int) {  
    val t = xs(i); xs(i) = xs(j); xs(j) = t  
  }  
  def sort1(l: Int, r: Int) {  
    val pivot = xs((l + r) / 2)  
    var i = l; var j = r  
    while (i <= j) {  
      while (xs(i) < pivot) i += 1  
      while (xs(j) > pivot) j -= 1  
      if (i <= j) {  
        swap(i, j)  
        i += 1  
        j -= 1  
      }  
    }  
    if (l < j) sort1(l, j)  
    if (j < r) sort1(i, r)  
  }  
  sort1(0, xs.length - 1)  
}
```

pivot
in the middle

explicitly
iterate

determine
when to swap



• Quicksort in Scala - functional programming

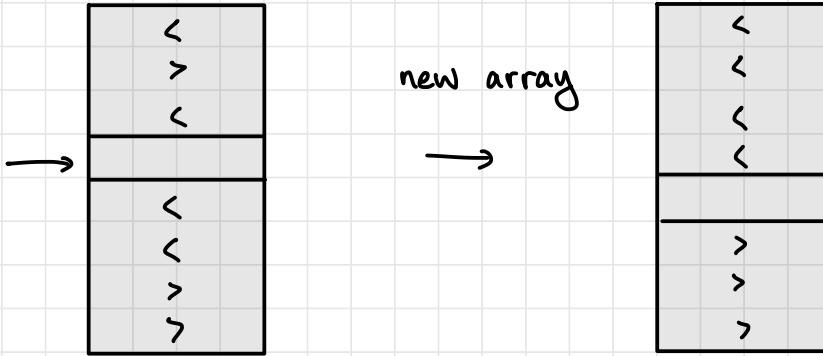
```
def sort(xs: Array[Int]): Array[Int] = {  
  if (xs.length <= 1) xs  
  else {  
    val pivot = xs(xs.length / 2)  
    Array.concat(  
      sort(xs filter (pivot >)),  
      xs filter (pivot ==),  
      sort(xs filter (pivot <))  
    )  
  }  
}
```

pick a pivot

sort values
smaller than
pivot

sort values
greater than
pivot

concatenate result



Q: Does this sort array in ascending order or descending order?

```
def sort(xs: Array[Int]): Array[Int] = {  
  if (xs.length <= 1) xs  
  else {  
    val pivot = xs(xs.length / 2)  
    Array.concat(  
      sort(xs filter (pivot >)),  
      xs filter (pivot ==),  
      sort(xs filter (pivot <))  
    )  
  }  
}
```

→ ascending

Q: Consider the program with array

`xs = 3,1,2,0,7,6,4,5`

Write a program to sort in the reverse order (if ascending, sort descending)

How can we parallelize this?

```
def sort(xs: Array[Int]): Array[Int] = {  
  if (xs.length <= 1) xs  
  else {  
    sort(xs filter (pivot <)),  
    xs filter (pivot ==),  
    sort(xs filter (pivot >)) } }  
}
```

can parallelise filtering tasks

Functional Programming & Functions

list remains unchanged

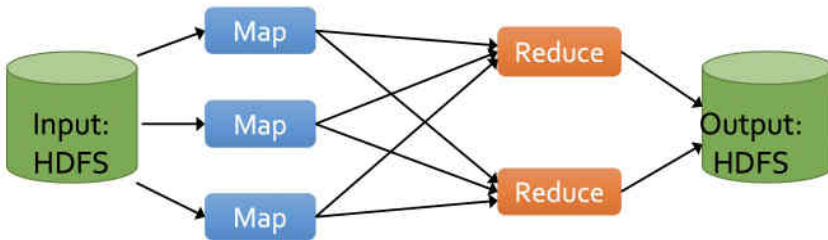
```
val list = List(1, 2, 3)  
list.foreach(x => println(x)) // prints 1, 2, 3  
list.foreach(println) // same  
  
list.map(x => x + 2) // returns a new List(3, 4, 5)  
list.map(_ + 2) // same  
  
list.filter(x => x % 2 == 1) // returns a new List(1, 3)  
list.filter(_ % 2 == 1) // same  
  
list.reduce((x, y) => x + y) // => 6  
list.reduce(_ + _) // same
```

Functional Programming & Big Data

- Independent parallel operations
 - `map()` in FP
- Parallel operations to be consolidated
 - `aggregation()` of FP

SPARK

- Most cluster prog models: DAG (Directed Acyclic Graph)



- Advantages of Hadoop
 1. Input HDFS → output HDFS
 2. User specified no. of M/R
 3. Handle failures
- Issues of Hadoop (think: page rank)
 1. Iterative
 2. Every iteration requires write to disk
 3. o/p of reducer → input of mapper (in & out of disk)
- Look: Hadoop

In-Memory Computation

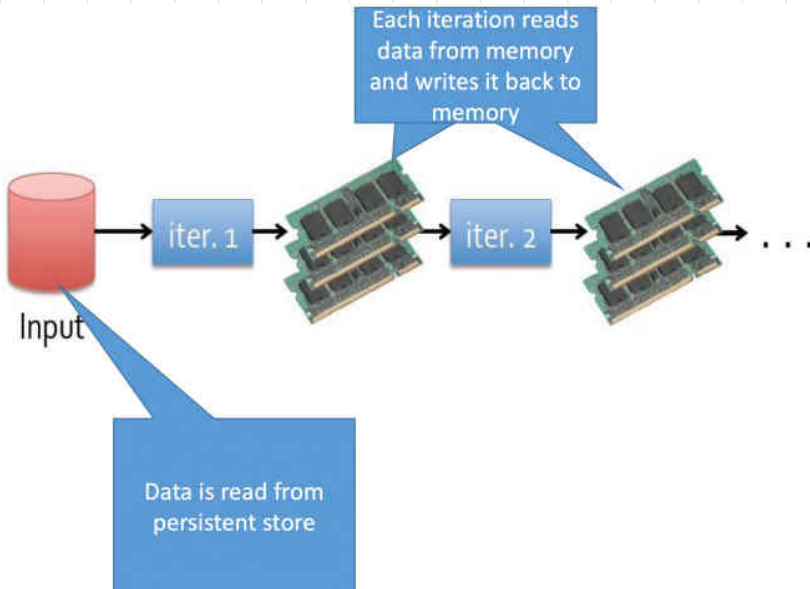
- Word-count program in Scala

```
val lines = scala.io.Source.fromFile("textfile.txt").getLines
val words = lines.flatMap(line => line.split(" ")).toIterable
val counts = words.groupBy(identity).map(words =>
    words._1 -> words._2.size) ———> compute word count
val top10 = counts.toArray.sortBy(_._2).reverse.take(10)
println(top10.mkString("\n"))
```

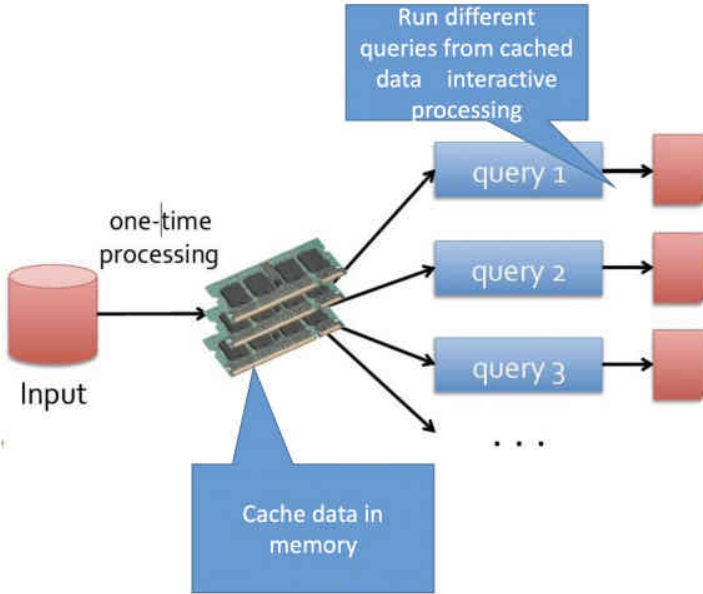
each operation creates
data value that can be
kept in memory & reused

Iterative Processing in Memory

- Think: page rank



• Caching



Problems

1. Too large for RAM ; how to deal with overflows
2. How to split across DRAM of entire cluster
3. How to handle failures (power failures)

DISTRIBUTED DATASET

- Flume: import logs into HDFS (error logs, activity logs etc)

Example Log Processing

- Load from log into memory
- Search for patterns

```
lines = spark.textFile("hdfs://...")
errors = lines.filter(startswithERROR())
messages = errors.map(split("\t"),2)
cachedMsgs = messages.cache()
```

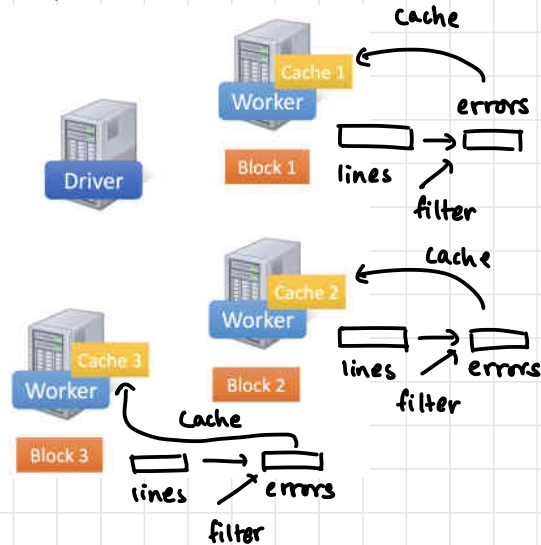
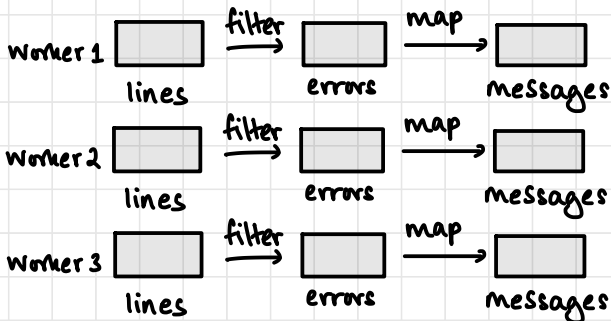
```
cachedMsgs.filter(containsfoo()).count()
cachedMsgs.filter(containsbar()).count()
```

Distribute the Computation

- lines: virtual DS with 3 parts (distributed)
- filter performed separately on each partition (parallelly)

```
lines = spark.textFile("hdfs://...")
errors = lines.filter(startswithERROR())
messages = errors.map(split("\t"),2)
cachedMsgs = messages.cache()
```

```
cachedMsgs.filter(containsfoo()).count()
cachedMsgs.filter(containsbar()).count()
```



Handling Fault Tolerance

Consider the following code:

```
Step1      Step2  
messages = textFile(...).filter(startswithERROR())  
                                .map(split("\t")(2))  
                                Step3
```

Step1: Read in the file to an in memory RDD

Step2: remove all lines that don't contain the term ERROR

Step3: split the line



map(func)

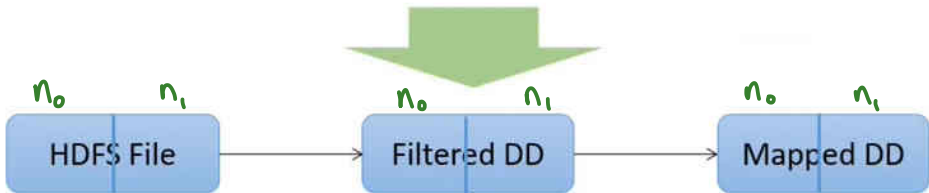
Return a new distributed dataset formed by passing each element of the source through a function *func*.

filter(func)

Return a new dataset formed by selecting those elements of the source on which *func* returns true.

• What if n_1 crashes after filter

```
messages = textFile(...).filter(startswithERROR())  
                                .map(split("\t")(2))
```



Resilient Distributed Dataset (RDD)

- Add lineage information to the concept of a distributed dataset
- Ability to recreate in case of failure
- Keep track of operations performed on RDD and to create RDD
- Types of operations support



RDD Operations

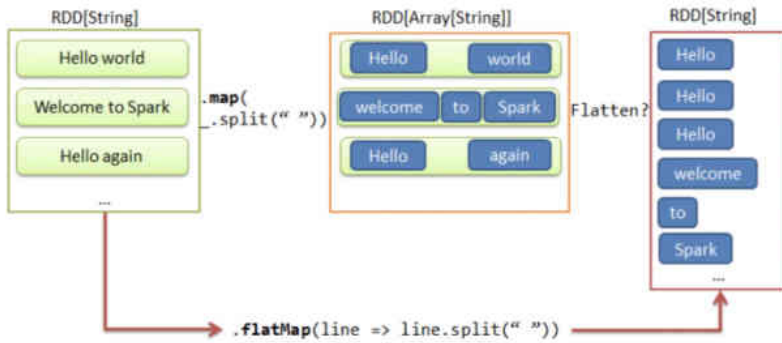
1. Transformations
2. Actions

Transformation

- Create new dataset from existing dataset
- Eg: `map()` in scala

Table 3-2. Basic RDD transformations on an RDD containing {1, 2, 3, 3}

Function name	Purpose	Example	Result
<code>map()</code>	Apply a function to each element in the RDD and return an RDD of the result.	<code>rdd.map(x => x + 1)</code>	{2, 3, 4, 4}
<code>flatMap()</code>	Apply a function to each element in the RDD and return an RDD of the contents of the iterators returned. Often used to extract words.	<code>rdd.flatMap(x => x.to(3))</code>	{1, 2, 3, 2, 3, 3, 3}
<code>filter()</code>	Return an RDD consisting of only elements that pass the condition passed to <code>filter()</code> .	<code>rdd.filter(x => x != 1)</code>	{2, 3, 3}
<code>distinct()</code>	Remove duplicates.	<code>rdd.distinct()</code>	{1, 2, 3}
<code>sample(withReplacement, fraction, [seed])</code>	Sample an RDD, with or without replacement.	<code>rdd.sample(false, 0.5)</code>	Nondeterministic



Q: $l = \{47, 39, 22, 25, 36\}$

$l.filter(x \Rightarrow (x \% 2) == 1)$

$47 \% 2 == 1 \longrightarrow \text{true}$

$39 \% 2 == 1 \longrightarrow \text{true}$

$22 \% 2 == 1 \longrightarrow \text{false}$

$25 \% 2 == 1 \longrightarrow \text{true}$

$36 \% 2 == 1 \longrightarrow \text{false}$

filtered = $\{47, 39, 25\}$

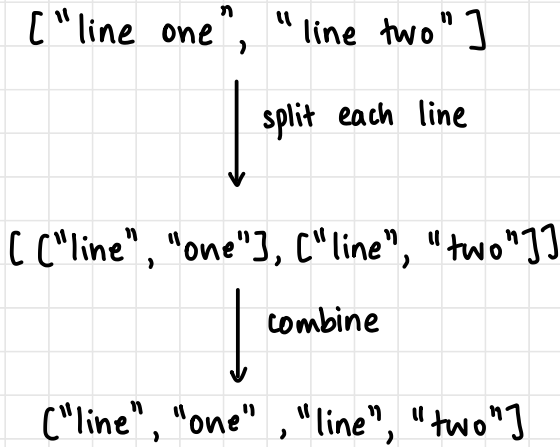
Q: $n_0 = \{47, 39, 22\}$ $n_1 = \{25, 36\}$

$l.filter(x \Rightarrow (x \% 2) == 1)$

$n_0 = \{47, 39\}$

$n_1 = \{25\}$

Flatmap



Transformations on 2 RDDs

Table 3-3. Two-RDD transformations on RDDs containing {1, 2, 3} and {3, 4, 5}

Function name	Purpose	Example	Result
union()	Produce an RDD containing elements from both RDDs.	rdd.union(other)	{1, 2, <u>3</u> , 3, 4, 5}
intersection()	RDD containing only elements found in both RDDs.	rdd.intersection(other)	{3}
subtract()	Remove the contents of one RDD (e.g., remove training data).	rdd.subtract(other)	{1, 2}
cartesian()	Cartesian product with the other RDD.	rdd.cartesian(other)	{{(1, 3), (1, 4), ..., (3,5)}

check if repeat is mistake

Actions

- Operations that return a value
- Eg: `reduce()`

Table 3-4. Basic actions on an RDD containing {1, 2, 3, 3}

Function name	Purpose	Example	Result
<u><code>collect()</code></u>	Return all elements from the RDD.	<code>rdd.collect()</code>	{1, 2, 3, 3}
<code>count()</code>	Number of elements in the RDD.	<code>rdd.count()</code>	4
<code>countByValue()</code>	Number of times each element occurs in the RDD.	<code>rdd.countByValue()</code>	{{(1, 1), (2, 1), (3, 2)}
<code>take(num)</code>	Return <code>num</code> elements from the RDD.	<code>rdd.take(2)</code>	{1, 2}
<code>top(num)</code>	Return the top <code>num</code> elements the RDD.	<code>rdd.top(2)</code>	{3, 3}
<code>takeOrdered(num)(ordering)</code>	Return <code>num</code> elements based on provided ordering.	<code>rdd.takeOrdered(2)(myOrdering)</code>	{3, 3}
<code>takeSample(withReplacement, num, [seed])</code>	Return <code>num</code> elements at random.	<code>rdd.takeSample(false, 1)</code>	Nondeterministic
<u><code>reduce(func)</code></u>	Combine the elements of the RDD together in parallel (e.g., sum).	<code>rdd.reduce((x, y) => x + y)</code>	9
<code>fold(zero)(func)</code>	Same as <code>reduce()</code> but with the provided zero value.	<code>rdd.fold(0)((x, y) => x + y)</code>	9

at master



at master



RDD Operations on Key-Value pairs

- Spark: pair RDDs

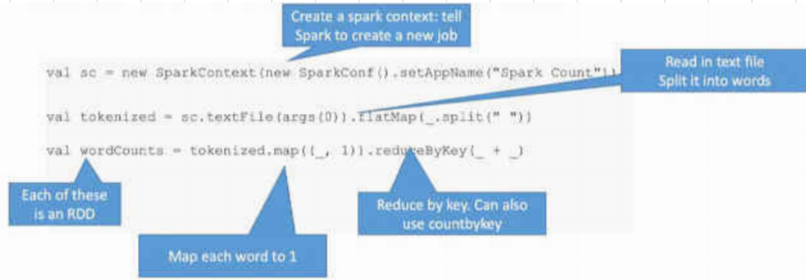
Table 4-1. Transformations on one pair RDD (example: $\{(1, 2), (3, 4), (3, 6)\}$)

Function name	Purpose	Example	Result
<code>reduceByKey(func)</code>	Combine values with the same key.	<code>rdd.reduceByKey((x, y) => x + y)</code>	$\{(1, 2), (3, 10)\}$
<code>groupByKey()</code>	Group values with the same key.	<code>rdd.groupByKey()</code>	$\{(1, [2]), (3, [4, 6])\}$
<code>combineByKey(createCombiner, mergeValue, mergeCombiners, partitioner)</code>	Combine values with the same key using a different result type.	See Examples 4-12 through 4-14.	
<code>mapValues(func)</code>	Apply a function to each value of a pair RDD without changing the key.	<code>rdd.mapValues(x => x+1)</code>	$\{(1, 3), (3, 5), (3, 7)\}$
<code>flatMapValues(func)</code>	Apply a function that returns an iterator to each value of a pair RDD, and for each element returned, produce a key/value entry with the old key. Often used for tokenization.	<code>rdd.flatMapValues(x => (x to 5))</code>	$\{(1, 2), (1, 3), (1, 4), (1, 5), (3, 4), (3, 5)\}$
<code>keys()</code>	Return an RDD of just the keys.	<code>rdd.keys()</code>	$\{1, 3, 3\}$
<code>values()</code>	Return an RDD of just the values.	<code>rdd.values()</code>	$\{2, 4, 6\}$

needs partition function

countByKey: distributed action
returns hashmap of (k, Int) pairs with count of
each key

WORD COUNT IN SPARK



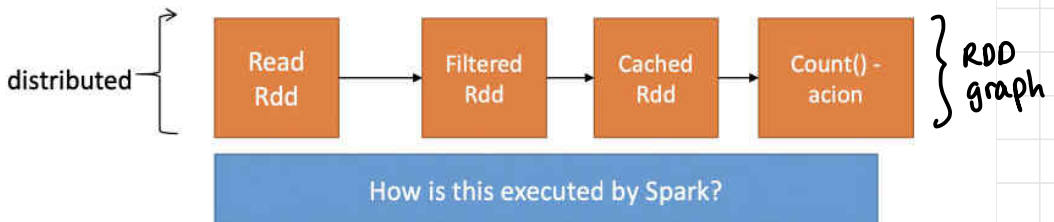
Spark Architecture

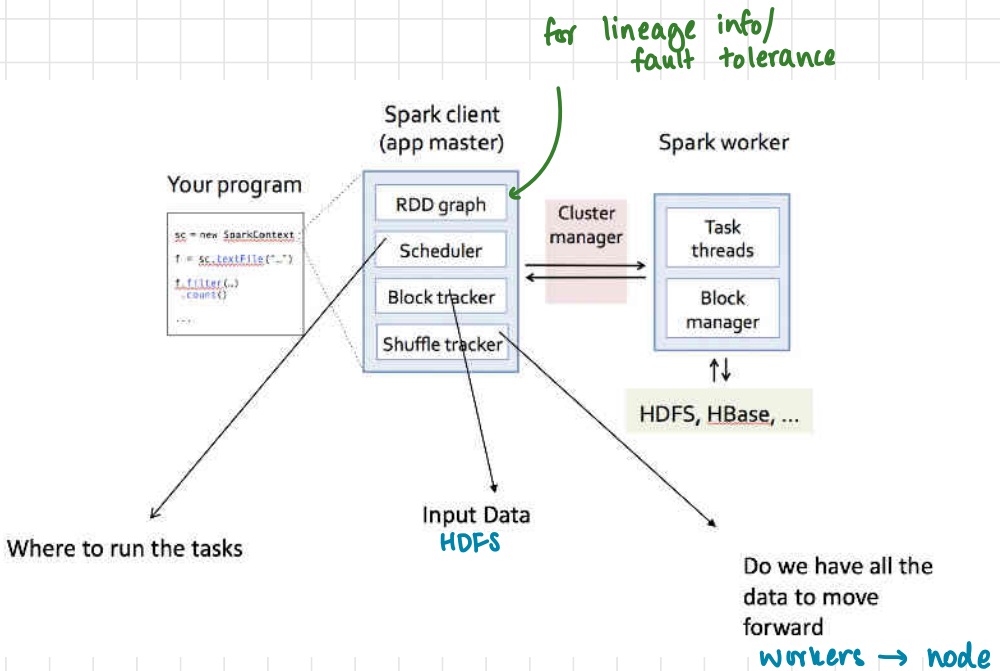
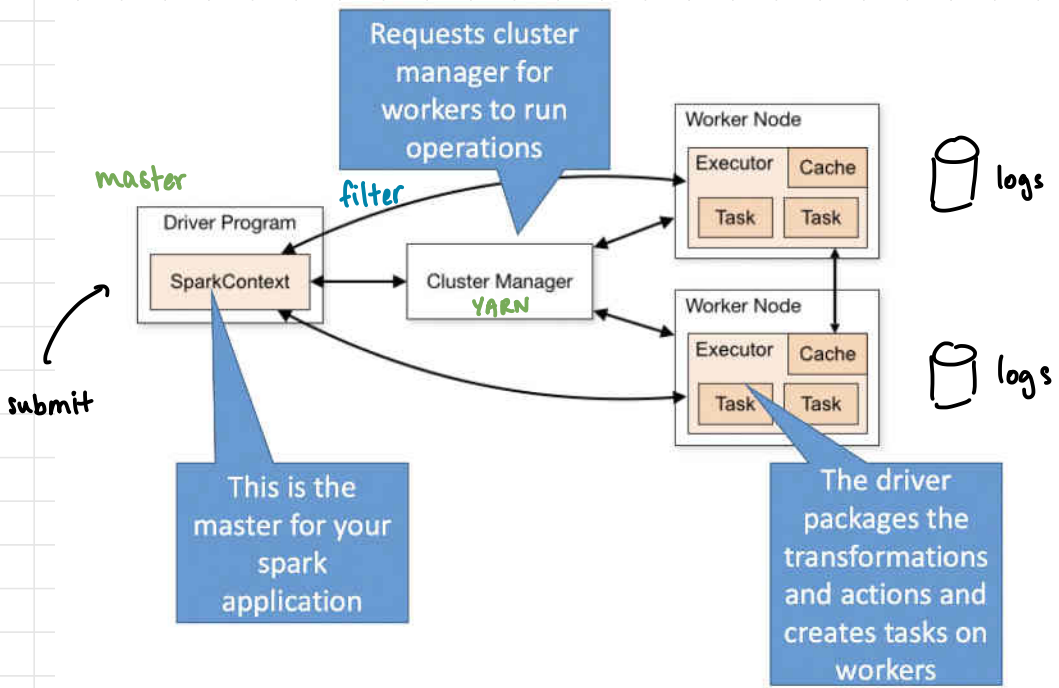
- Eg: log mining

```
val sc = new SparkContext("spark://...", "MyJob", home, jars)
val file = sc.textFile("hdfs://...") // This is an RDD
val errors = file.filter(_.contains("ERROR")) // This is an RDD
errors.cache()
errors.count() // This is an action
```

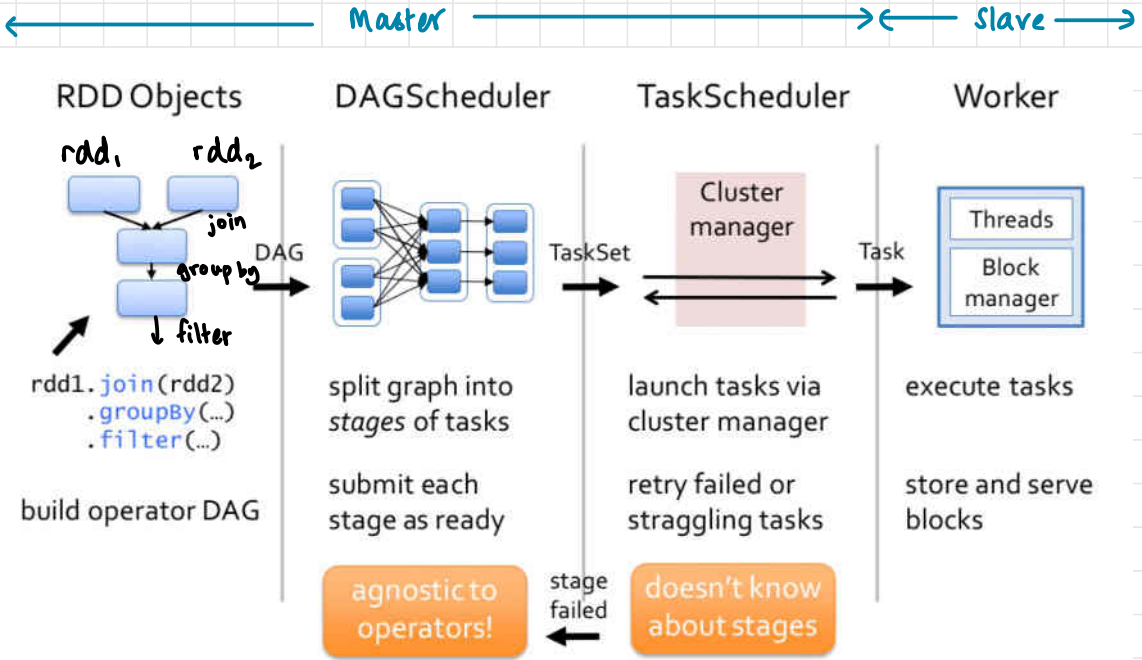
Annotations:

- cache: in order to replicate if fails, reduce processing time, retain for further use (prevent garbage collect)



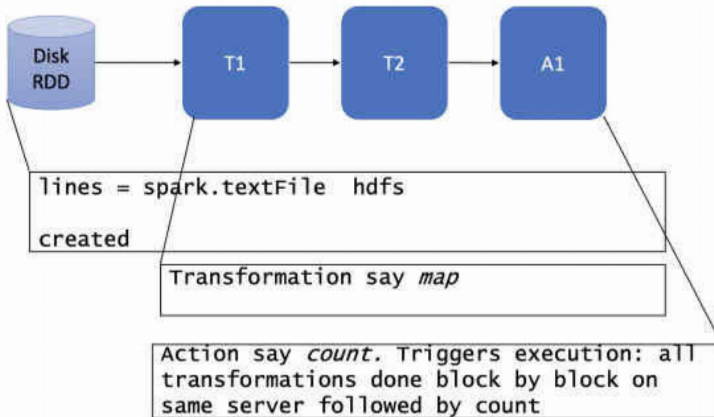


Spark Working Details



Lazy Execution

- Spark driver: no execution when encounters a transformation
- Transformations only noted for lineage
- Executes only when action encountered



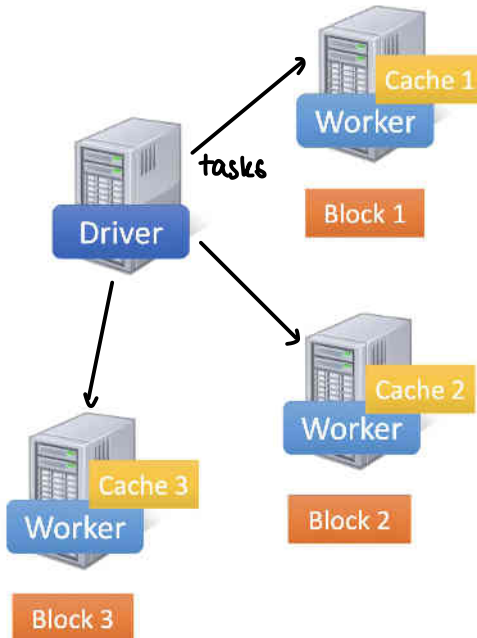
Q: Why lazy execution?

- Clustering transformations reduce net traffic
- Bring data into memory once
- Optimisations can be performed

Spark Log Mining Example

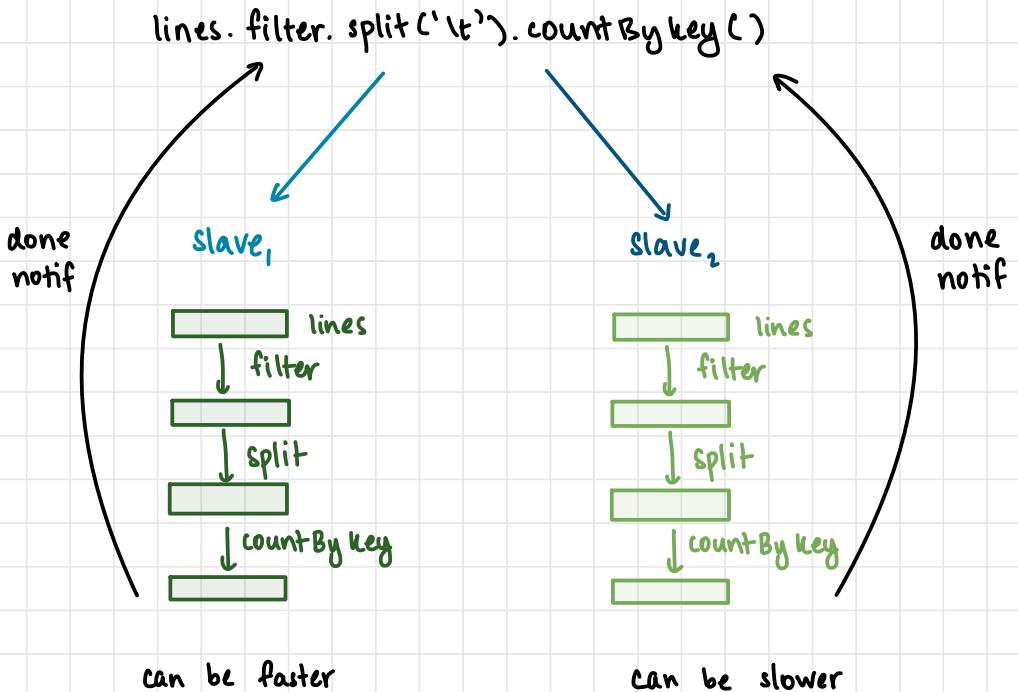
parallel {
lines = spark.textFile("hdfs://...") → base RDD
errors = lines.filter(startsWith(ERROR()))
messages = errors.map(split("\t"), 2) → transformed RDD
cachedMsgs = messages.cache()

cachedMsgs.filter(containsfoo()).count() → action
cachedMsgs.filter(containsbar()).count()



RDDs- Details

- Partitioned, locality aware, distributed collection
- RDDs are immutable (no partial state with multiple threads)
- RDDs are DS that either
 - point to data source (HDFS)
 - apply a transformation to parent RDDs to generate new elements
- Computations on RDDs
 - lazily evaluated lineage DAGs composed of chained RDDs

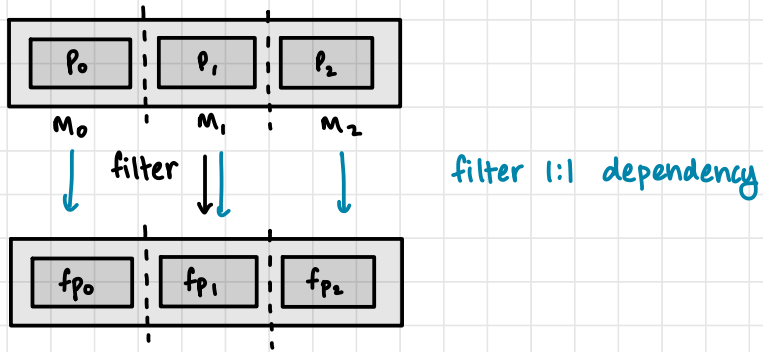


Why RDD Abstraction?

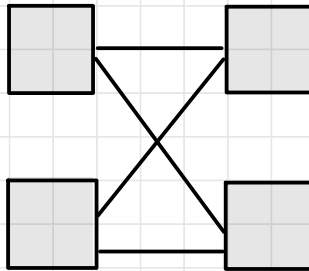
- Support operations other than MR
- Support in-memory computation
- Arbitrary composition of such operators
- Simplify scheduling (order of generation of RDDs)

Representing RDDs

- Splits — set of partitions (machines)
 - like Hadoop, each RDD associated with input partition



MR:



- List of dependencies on parent RDDs
- Function to compute partitions given parents
- Optional preferred locations
- Optional partitioning info (partitioner for shuffle)

RDDs Interface

Operation	Meaning
<code>partitions()</code>	Return a list of Partition objects
<code>preferredLocations(p)</code>	List nodes where partition p can be accessed faster due to data locality
<code>dependencies()</code>	Return a list of dependencies
<code>iterator(p, parentIters)</code>	Compute the elements of partition p given iterators for its parent partitions
<code>partitioner()</code>	Return metadata specifying whether the RDD is hash/range partitioned

Hadoop RDD (map)

Partitions - one per block

Dependencies - none

Compute (partition) - read corresponding block

Preferred locations - HDFS block location

Partitioner - none

Filtered RDD

Partitions - same as parent

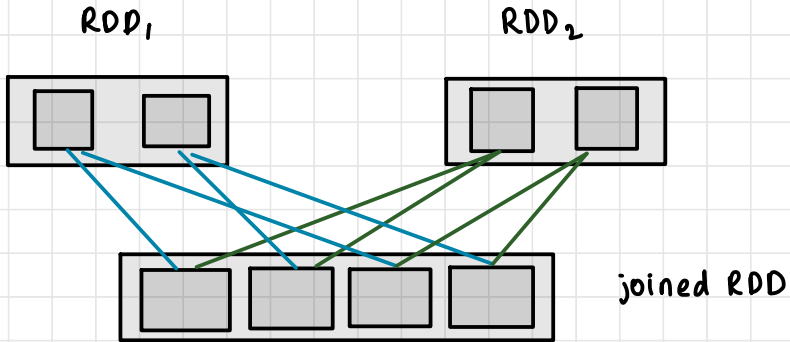
Dependencies - 1-1 with parent

Compute - compute parent and filter it

Preferred locations - ask parent (none)

Partitioner - none

Join RDD



Partitions - one per reduce task

Dependencies - many to one

Compute - read and join shuffled data

Preferred locations - none

Partitioner - HashPartitioner

ReduceByKey RDD

- Transformation

Partitions - one per key

Dependencies - many to many (on all parent nodes)

Compute - reduce data and send

Preferred locations - subset of parent partitions involved

Partitioner - hash

x_1	v_1
x_2	v_2
x_3	v_3

x_1	v_4
x_4	v_5

Spark Scheduling

Page Rank in Spark

urls → link
(source) (dest)

```
lines = textfile
links = lines.map(lambda urls: urls.split()).groupByKey().cache()
ranks = links.map(lambda url_neighbors: (url_neighbors[0], 1.0))

for iteration in range(MAXITER):
    contribs = links.join(ranks).flatMap(lambda url_neighbors_rank:
        computeContribs(url_neighbors_rank))

    ranks = contribs.reduceByKey(add).mapValues (lambda rank: rank *
        0.85 + 0.15)
```

```
def computeContribs (url_neighbors_rank):
    """Calculates URL contributions to the rank of other URLs.
    """

    num_neighbors = len (url_neighbors_rank) - 1
    rank = url_neighbors_rank [len (url_neighbors_rank) - 1]

    for i in range (1, num_neighbors):
        yield (url_neighbors_rank[i], rank / num_neighbors)
```



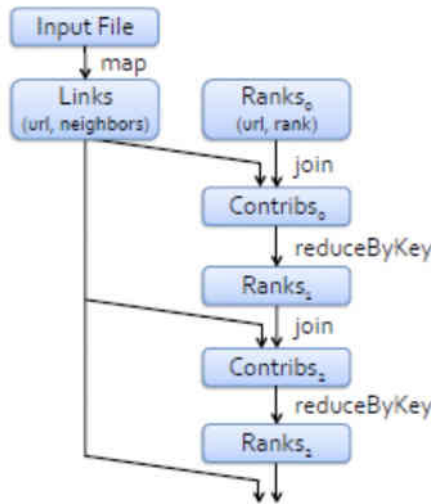
DAG Representation

```
lines = textfile("urls.txt")
links = lines.map (lambda urls: urls.split()).groupByKey().cache()

ranks = links.map(lambda url_neighbors: (url_neighbors[0], 1.0))

for iteration in range(MAXITER):
    contribs = links.join(ranks).flatMap(lambda url_neighbors_rank:
    computeContribs(url_neighbors_rank))

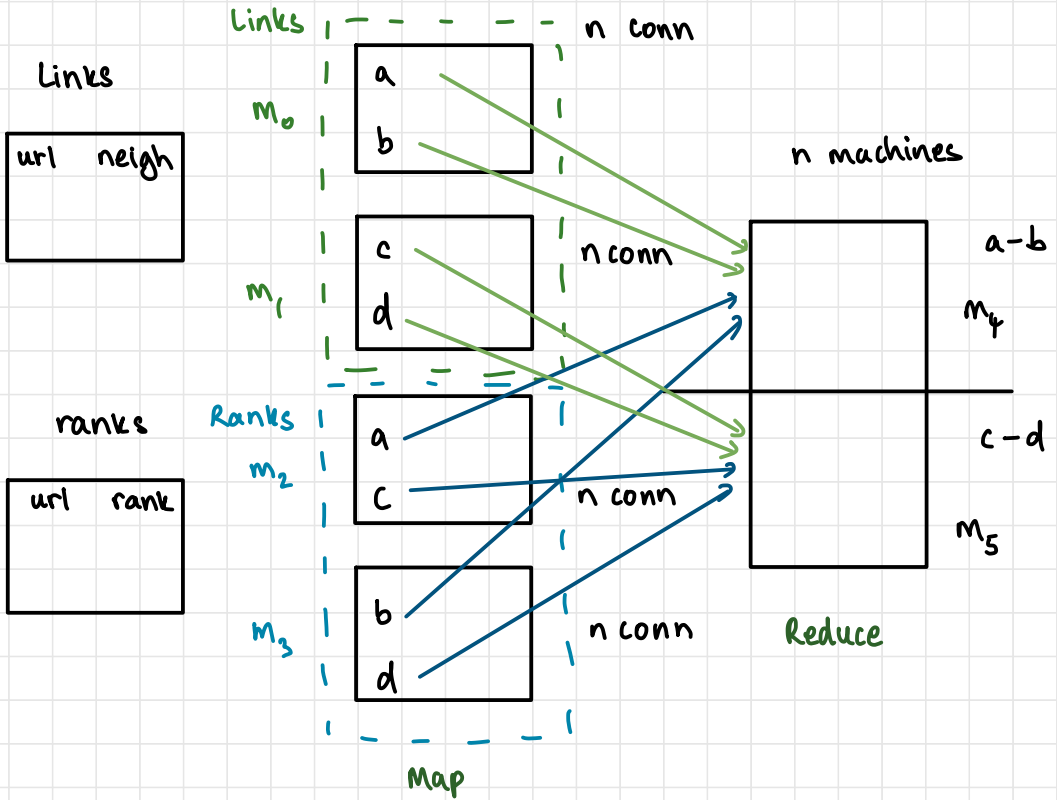
    ranks = contribs.reduceByKey(add).mapValues(lambda rank:
    rank*0.85 + 0.15)
```



Note: ranks & links spread across multiple nodes. How does spark ensure join works properly?

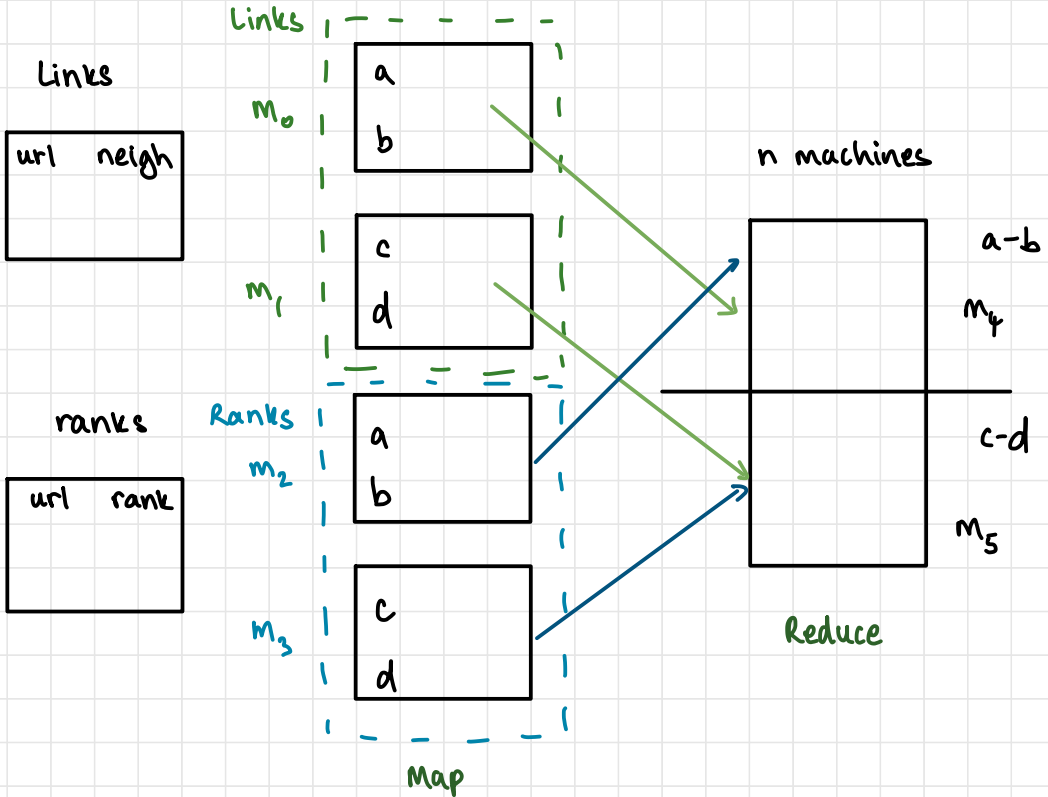
Links join Ranks

- wide dependency



- Requires full shuffle over network
- Each worker depends on all parents
- Make more efficient?
 - copartition
- If Links & Ranks partitioned with same function

- Narrow dependency



Wide & Narrow Partitioning

1. Narrow

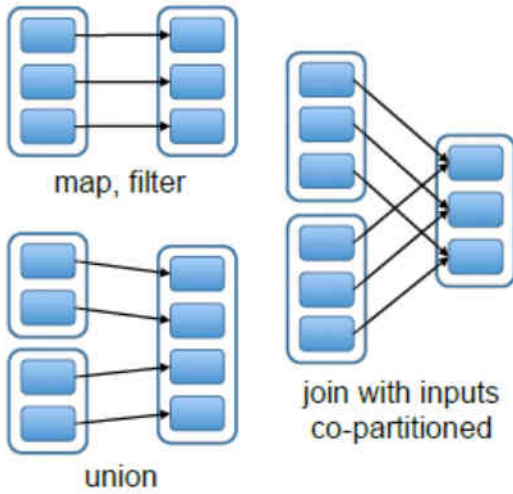
- each partition of parent RDD used by at most one partition of child RDD
- No shuffle; pipeline operations

2. Wide

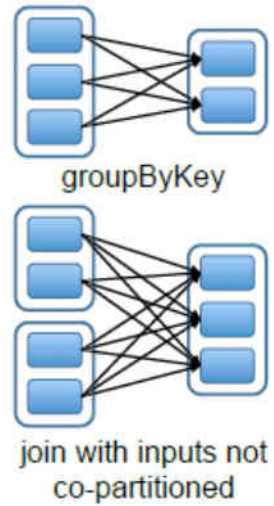
- multiple child partitions may depend
- shuffle

Copartition: both join inputs partitioned with same function

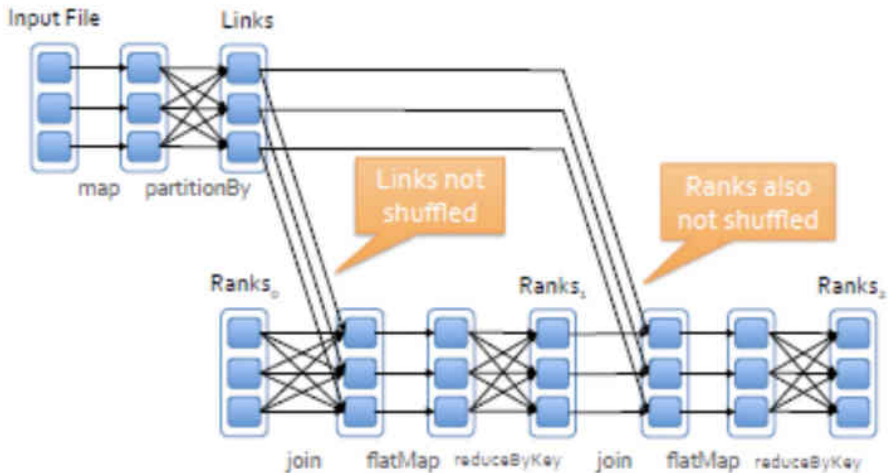
Narrow Dependencies:



Wide Dependencies:



Lineage & Optimising Placement



Narrow

Wide

Map

FlatMap

MapPartitions

Filter

Sample

Union

Intersection

Distinct

ReduceByKey

GroupByKey

Join

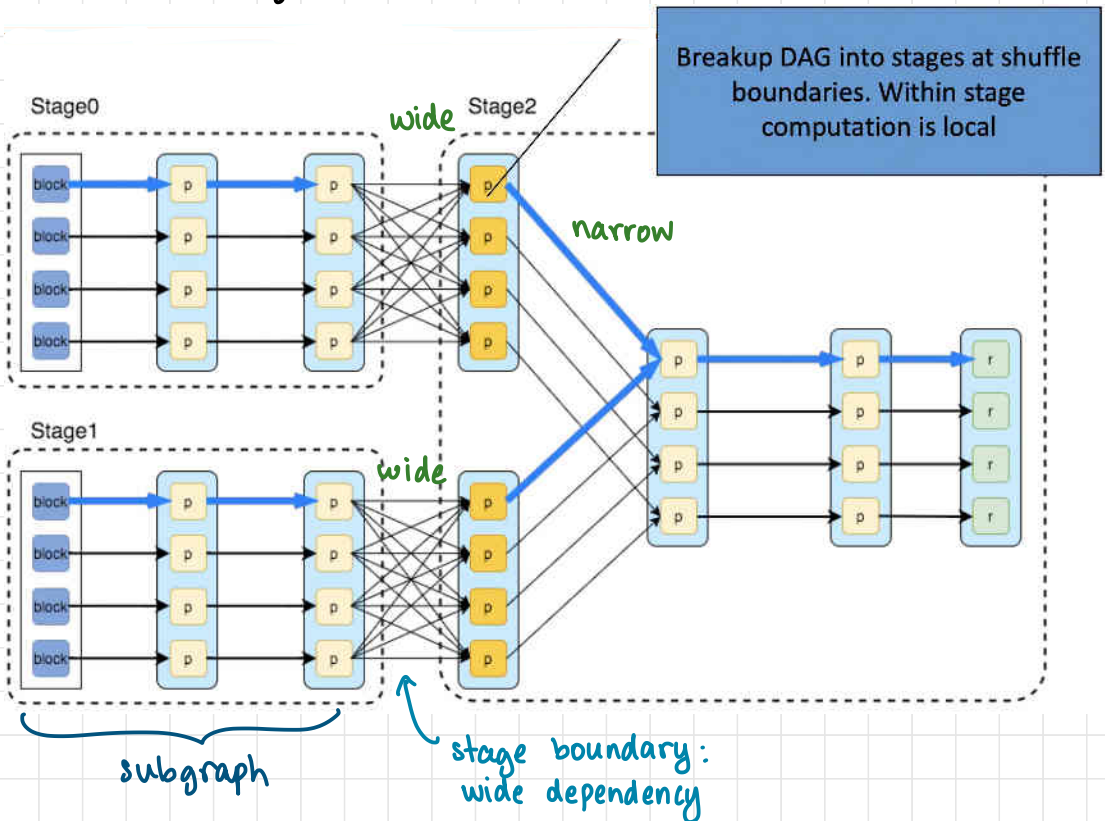
Cartesian

Repartition

Coalesce

Scheduling

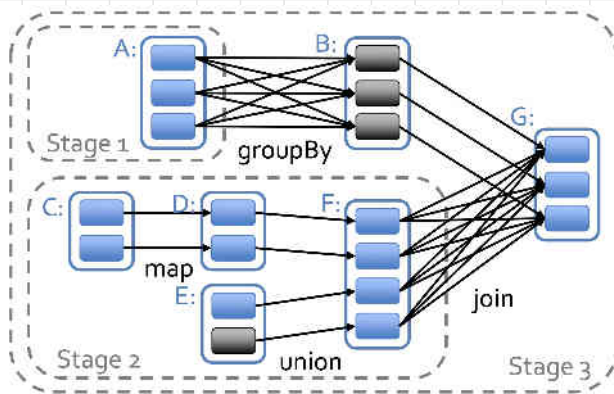
- subgraphs separated by wide partition
- within stages: local



- S_0 and S_1 can be scheduled in parallel
- S_2 only after S_0 & S_1 complete

TASK ASSIGNMENT

- Scheduler assigns tasks to machines based on data locality using delay scheduling



- If partition to be processed available in memory on a node, sent to that node
- Otherwise, task processes partition for which the containing RDD provides preferred location and sends to those

Dataframes

- RDDs opaque to Spark → cannot parse
- Spark must understand format

- Distributed collection of data into named columns (abstraction over RDDs)

```
from pyspark.sql import SQLContext

sqlContext = SQLContext(sc)

# DataFrames can be created from existing RDDs,
# HIVE tables or other data sources.
# Here, from JSON file
df = sqlContext.jsonFile("pes/students.json")

# Display the contents
df.show()

## USN   name   marks
## 045   Vkoli   11
## 010   Stendul  43
## 195   Abachpan28

# Alternatively, from an existing RDD by naming
# the columns
Df = rdd.toDF("USN", "name")
```

Using DataFrame

```
# Print the schema in a tree format
df.printSchema()
## root
## |-- usn: long (nullable = true)
## |-- name: string (nullable = true)
## |-- marks: long (nullable = true)

# Select only the "name" column
df.select("name").show()
## name
## VKoli
## STendul
## ABachpan

# Select everybody, but increment the age by 1
df.select("name", df.marks + 1).show()
## name      (marks + 1)
## VKoli      12
## STendul    44
## ABachpan   29
```

Q: Consider a case where you have data in a CSV file that consists of `<pan_number, date, tax_paid>` and you wanted to find out the total tax paid by each individual pan holder

(a) How will you do it in Spark?

(b) How will you do it with Spark Data frames?

(a) `reduce By Key (x,y) => x+y` *key = pan-number*

(b) `select sum(tax-paid) from df group by pan-number`
(pseudocode)

```
df = rdd.toDF("pan_number", "date", "tax paid")
```

```
df.select("pan_number", "tax_paid").groupBy("pan_number").sum()
```

Other Tools

- Spark always preferred

DryadLINQ, FlumeJava

- Similar "distributed collection" API but cannot reuse datasets efficiently across queries

Relational databases

- Lineage/provenance, logical logging, materialized views

GraphLab, Piccolo, BigTable, RAMCloud

- Fine-grained writes similar to distributed shared memory

Iterative MapReduce (e.g. Twister, HaLoop)

- Implicit data sharing for a fixed computation pattern

Caching systems (e.g. Nectar)

- Store data in files, no explicit control over what is cached

Big Data Algorithm Complexity

Q: Complexity of matrix multiplication on single node?

$$\sum_{i=1}^n \sum_{j=1}^n \sum_{k=1}^n 1 = O(n^3) \quad \text{--- complexity depends on no of computations}$$

Q: Complexity of database query?

hashtable — amortised $O(1)$ } in-memory
bst / rbt — $O(\log n)$

complexity depends on disk reads

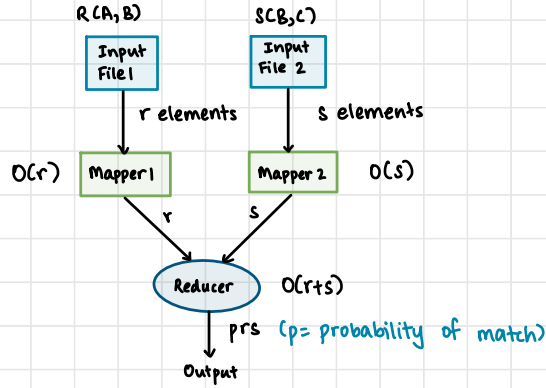
Cost of BD Algorithms

- Algorithms tend to be $O(n)$ (map-reduce)
- Network speed \ll CPU speed
- Disk speed \ll CPU speed
- Majorly impacted by communication time

Communication Cost

- Depends on input size
- Final o/p usually smaller by aggregation

Q: Complexity of natural join of R, S



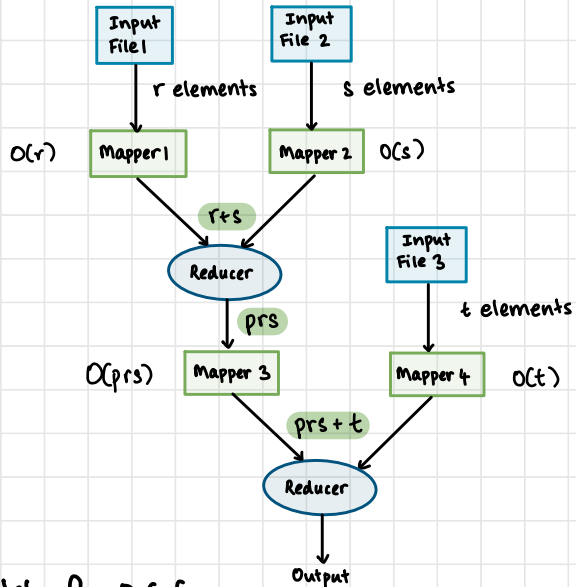
Mapper I/P complexity: $r+s$

Reducer I/P complexity: $r+s$

Total complexity: $O(r+s)$

Q: Complexity of natural join of R, S, T

Case 1:



rs : complexity of cartesian prod

Let p = probability of match for $R \Join S$

total cost = $O(r+s+t+prs)$

Case 2: join S, T and then R

Let $q =$ prob of join of S, T

Total cost: $O(r+s+t+qst)$

If $p \sim q$, join $\min(rs, st, rt)$

Wall Clock Time

- Time taken for entire job to finish
- Linux: `time ls /bin`
 - real: wall clock time
 - user: time CPU spends executing user code
 - sys: time CPU spends executing system (OS) code

Trade-off — Parallelism

- Dividing tasks: reduce wall clock time, increase communication time
- Reducer size q (not no. of reducers)
 - no of unique values with same key
- No of map o/p's T
- q small, more reducers
 - max reducers T/q
 - reduce WCT, increase CT
- Replication rate r
 - $r = (\text{no of kv pairs in mapper o/p}) / (\text{no of input records to mapper})$
 - \propto avg CT from M tasks to R tasks

Wall Clock Example - SIMILARITY JOIN BETWEEN IMAGES

- DB of 10^6 images, 1 MB each (1TB DB)
- Similarity function $s(x,y)$ on images x and y such that $s(x,y) = s(y,x)$
- Output all x,y st $s(x,y) > t$

Naive Algorithm

- Each image P_i has index i
- Mapper
 - reads (i, P_i)
 - generates all possible pairs $(\{i, j\}, \{P_i, P_j\})$ ($i \neq j$)
- Reducer
 - reads $(\{i, j\}, \{P_i, P_j\})$
 - computes $s(P_i, P_j)$
- Communication cost of naive algorithm?
 - $O(n^2)$ where n = no. of images (to generate pairs)
- Parallelism of naive algorithm
 - potentially very high as reducer size very high & each can be processed in parallel
- Replication rate of naive algorithm?
 - $O(P)$ of mapper / $1/P$ to mapper
 - $O(n)$

Alternate Solution (Low Communication Cost)

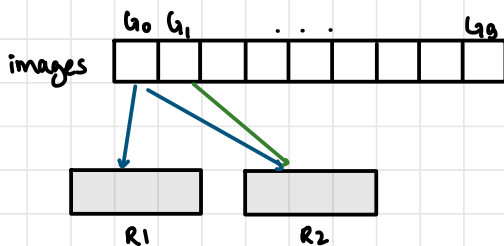
- Reducer runs on same node as mapper
- Very low parallelism

Summary - 2 Choices

1. One pair to each reducer
 - High communication cost (bad)
 - High parallelism (good)
2. Do everything on one node
 - Low parallelism (bad)
 - Low communication cost (good)
3. Something in between?

Group-Based Algorithm

- Group images



Suppose the groups are G_0 ,

Group G_0 is sent to nodes 0, 1, ..., 98

Why?

Group G_0 has to be compared with 99 other groups

Group G_1 is sent to?

—0, 1, —

Group G_1 is sent to 0, 99, 100, ...196 (0+98 other nodes)

Group G_2 is sent to?

Group G_2 is sent to 1, 99, 197, 198, ... 293 (1, 99 +97 other nodes)

Group G_3 is sent to 2, 100, 197, 294, ...389 (2, 100, 197, +96 other nodes)

- No. of groups = g
- No. of images per group = $m = n/g$
- Each group sent to $g-1$ servers
- Total no. of messages = $g(g-1)$
- Total data = $mg(g-1) = n(g-1) \sim ng = CC$
- Parallelism = no. of nodes = $(g-1) + (g-2) + (g-3) + \dots = \frac{g(g-1)}{2} = O(g^2)$
- Or, no. of nodes = ${}^n C_2 = \frac{g(g-1)}{2}$

Q: Suppose we have groups of 100

(a) How many groups are there?

(b) How many nodes is each group sent to?

What is the

(i) Communication cost of the algorithm?

(ii) Parallelism of the algorithm?

(a) 10^6 images, 10^2 per group = 10^4 groups

(b) Each group sent to $10^4 - 1$ nodes

(i) $CC = ng = 10^6$ images $\times 10^4$ groups = 10^{10}

(ii) parallelism $\sim (10^4)^2 = 10^8$